INTERMEDIATE WATER AND WASTEWATER MATH

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Math Problem Solving Strategy

- 1. Read the question carefully and underline what they are asking you to find.
- 2. Write down the formula you need to solve the problem. Look in the front of the test booklet if necessary.
- 3. Fill in everything you know. Sometimes filling in what you know might require you to find something else first like area or volume.
- 4. Check your units! Make sure they are correct for the formula and agree with each other.
- 5. Convert units where needed.
- 6. Put the new units into the formula.
- Solve.
- 8. Check the units of your answer. Are they what the question asked for?
- 9. Convert units if necessary.

Unit Conversions

- 1. Convert 20 gpm to mgd
- 2. Convert 60 mph to ft/second
- 3. Convert 6000 cf to gallons
- 4. Convert 7 days into seconds
- 5. Convert 120 feet of static head into psi
- 6. Convert 14 acres into square feet
- 7. Convert 3 cubic yards into gallons
- 8. Convert 1 acre-ft/day into gpm
- 9. Convert 15 cfs into gpm
- 10. Convert 3 mgd to cfs
- 11. Convert 400 psi into feet of head
- 12. Convert 30 HP into kW. If this piece of equipment runs for 80 hours and electricity costs \$0.07 per kilowatt hour, what will it cost?
- 13. Convert 144 square inches into square feet
- 14. Convert 20 gal/sf to liters per square meter
- 15. A tank contains 20 feet of water and is 10 feet in diameter. What is the pressure in psi at the bottom of the tank?

Tank Geometry

- 16. The diameter of a wet well is 10 feet. If filled to a depth of 12 feet, it will contain approximately how many gallons of water?
- 17. How many gallons of liquid can be held by a tank that measures 40 feet long by 25 feet wide by 12 feet deep?
- 18. Approximately how many gallons would 600 feet of 6-inch diameter pipe hold?



- 19. A cylindrical water tank must be painted both inside and out. All surfaces, except the bottom of the tank where it contacts the ground, must be painted. If the tank is 20 feet tall and 60 feet in diameter, how many square feet must be painted?
- 20. A water storage tank holds 323,136 gallons. If the water depth in the tank is 12 feet, what is the area of the tank is square feet?
- 21. The inside walls and bottom of a concrete tank must be painted. The floor of the tank is 25 feet long by 15 feet wide. If the tank is 12 feet deep and does not have a top, how many square feet must be painted?
- 22. How many gallons does a 400 foot long section of 24-inch pipe hold?

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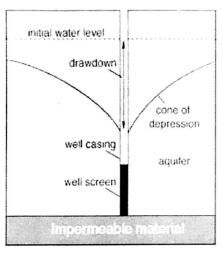
- 23. The distribution system has 3 storage tanks. Each tank is 50 feet square and 30 feet deep. What is the maximum storage volume of the distribution system in gallons?
- 24. Find the perimeter of a circular sedimentation basin if the basin is 30 feet in diameter.
- 25. A 24 foot diameter tank has a conical bottom. The sidewater depth (top of cone to water surface level) is 20 feet. The cone is 6 feet deep at its deepest point. What is the volume of the cone in cubic feet?

Hydraulic Retention Time

- 26. A tank holds 500 gallons. A pump is used to fill the tank at a rate of 25 gpm. How long will it take to fill the tank?
- 27. A finished water storage tank is 35 feet in diameter and 65 feet high. With no water entering the tank, the water level dropped 14 feet in 5 hours. Find the average rate of flow for water leaving the tank in gallons per minute.
- 28. If two pumps transfer 120 gpm each, how long will it take to fill a tank 50 feet long, 20 feet wide, and 8 feet deep? Express your answer in hours and minutes.
- 29. What is the average detention time in a basin given the following: diameter is 65 feet, depth is 12 feet, influent flow is 700 gpm.
- 30. A settling basin that is 60 feet long, 15 feet wide, and 12 feet deep is used to treat a flow of 2.4 mgd. What is the detention time?
- 31. What is the detention time in days for a reservoir if the influent flow rate is 0.785 mgd, the reservoir covers 17 acres, and has an average depth of 22 feet?



- 32. A water main feeds a subdivision. The main is 500 feet long and 12-inches in diameter. The pipe delivers an average flow of 30 cfm. The distribution crew is flushing the main to remove sediment. How long should they flush the line to achieve 2 pipe volumes?
- 33. A rectangular basin measures 100 feet long by 50 feet wide by 12 feet deep. A pump drawing water out of the tank is able to empty the tank in 1.24 days. What is the pump rate in gpm?
- 34. Determine the flow capacity of a pump in gpm if the pump lowers the water is a six-foot square wet well by 8 inches in 5 minutes.



Wells

- 35. A well is drilled through an unconfined aquifer. The top of the aquifer is 80 feet below grade. After the well was in service for a year, the water level in the well stabilized at 110 feet below grade. What is the drawdown?
- 36. A well produces 300 gpm. If the drawdown is 30 feet, find the specific yield.
- 37. The specific yield for a well is 10 gpm/ft. If the well produces 550 gpm, what is the drawdown?
- 38. The pumped water level of a well is 400 feet below the surface. The well produces 350 gpm. If the aquifer level is
- 250 feet below the surface, what is the specific yield for the well?

Force

- 39. Find the force on a 12-inch valve if the water pressure within the line is 60 psi. Express your answer in tons.
- 40. A 42-inch main line has a shut off valve. The same line has a 10-inch bypass line with another shut-off valve. Find the amount of force on each valve if the water pressure in the line is 80 psi. Express your answer in tons.
- 41. A water tank is 15 feet deep and 30 feet in diameter. What is the force exerted on a 6-inch valve at the bottom of the tank?

Velocity

42. A 42-inch diameter pipe transfers 35 cubic feet of water per second. Find the velocity in ft/sec.

43. A plastic float is dropped into a channel and is found to travel 10 feet in 4.2 seconds. The channel is 2.4 feet wide and 1.8 feet deep. Calculate the flow rate of water in cfs.

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- 44. The flow velocity of a 6-inch diameter pipe is twice that of a 12-inch diameter pipe if both are carrying 50 gpm of water. True or false?
- 45. What should the flow meter read in gpm if a 4-inch diameter main is to be flushed at a velocity of 4.6 fps?
- 46. The velocity through a channel is 4.18 fps. If the channel is 4 feet wide by 2 feet deep by 10 feet long, what is the flow rate in gpm?
- 47. What is the average flow velocity in ft/sec for a 12-inch diameter main carrying a daily flow of 2.5 mgd?

Pumps

- 48. Water is being pumped from a reservoir to a storage tank on a hill. The elevation difference between water levels is 1200 feet. Find the pump size required to fill the tank at a rate of 120 gpm. Express your answer in horsepower.
- 49. A 25 hp pump is used to dewater a lake. If the pump runs for 8 hours a day for 7 days a week, how much will it cost to run the pump for one week? Assume energy costs \$0.07 per kilowatt hour.
- 50. A pump station is used to lift water 50 feet above the pump station to a storage tank. The pump rate is 500 gpm. If the pump has an efficiency of 85% and the motor has an efficiency of 90%, find each of the following: Water Horsepower, Brake Horsepower, Motor Horsepower, and Wire-to-Water Efficiency.
- 51. A chemical feed pump with a 6-inch bore and a 6-inch stroke pumps 60 cycles per minute. Find the pumping rate in gpm.
- 52. Determine the flow capacity of a pump in gpm if the pump lowers the water level in a 6-foot square wet well by 8 inches in 5 minutes.
- 53. Find the brake horsepower for a pump given the following information: Total Dynamic Head = 75 feet, Pump Rate = 150 gpm, Pump Efficiency = 90%, Motor Efficiency = 85%
- 54. How much will it cost to run the pump in #53 for one year if the pump runs 12 hours a day, 365 days a year? Assume energy costs \$0.08 per kilowatt hour.
- 55. A single-piston reciprocating pump has a 4-inch diameter piston and an 8-inch stroke length. If makes 16 discharge strokes per minute. Find the pumping rate in gpm.



56. After calibrating a chemical feed pump, you've determined that the maximum feed rate is 178 mL/ minute. If this pump ran continuously, how many gallons will it pump in a full day?

Disinfection and Chemical Dosing

- 57. Determine the chlorinator setting in pounds per day if a water plant produces 300 gpm and the desired chlorine dose is 2.0 mg/L.
- 58. The finished water chlorine demand is 1.2 mg/L and the target residual is 2.0 mg/L. If the plant flow is 5.6 mgd, how many pounds per day of 65% hypochlorite solution will be required?
- 59. Fluoride is added to finished water at a dose of 4 mg/L. Find the feed rate setting for a fluoride saturator in gal/min if the water plant produces 5 mgd.
- 60. If chlorine costs \$0.21 per pound, what is the daily cost to chlorinate a 5 mgd flow rate at a dosage of 2.6 mg/L?
- 61. One gallon of sodium hypochlorite laundry bleach, with 5.25% available chlorine, contains how many pounds of active chlorine?
- 62. How much sodium hypochlorite, in gallons, is required to obtain a residual of 100 mg/L in a well? The casing diameter is 18-inches and the length is 80 feet. Sodium hypochlorite contains 5.25% available chlorine. Assume a demand of 15 mg/L.
- 63. A water company uses an average of 600 gpm of water. The water contains 0.30 mg/L of manganese and 0.06 mg/L of iron. How many pounds of iron and manganese are pumped into the distribution system each year?
- 64. How many pounds of copper sulfate will be needed to dose a reservoir with 0.6 mg/L of copper? The reservoir holds 30 million gallons. The copper sulfate is 25% copper by weight.
- 65. Liquid alum delivered to a water treatment plant contains 642.3 milligrams of aluminum per milliliter of liquid solution. Jar tests indicate that the best alum dose is 9 mg/L. Determine the setting on the liquid alum feeder in ml/min when the plant flow is 3.2 mgd.
- 66. The raw water supply contains 1.8 mg/L of fluoride. The flow rate is 400 gpm. The target fluoride dose for the finished water is 3 mg/L. Find the desired feed rate in gpm for a fluoride saturator.
- 67. The raw water alkalinity is 50 mg/L as calcium carbonate. The water is treated by adding 15 mg/L of alum. What is the alkalinity of the finished water?

Filters

- 68. A water plant has three filters. Each filter is 12 feet wide by 12 feet long. Find the hydraulic loading rate in gpm/sf when all three filters are on-line and the raw water enters the plant at 9.5 mgd.
- 69. A sand filter will be backwashed at a rate of 8 gpm/sf. If the filter is 10 feet wide by 15 feet long, what will the filter backwash rise rate be in inches per minute?
- 70. A series of filters must be backwashed. Each filter is 20 feet square. If the goal is to achieve a filter backwash rise rate of 30 inches per minute, what should the backwash rate be in gpm/sf?
- 71. A water plant has 3 filters. The plant is currently treating 5 mgd. If each filter is 12 feet wide by 20 feet long, what is the minimum number of filters that should be placed into service to keep the hydraulic loading rate below 20 gpm/sf?
- 72. Find the yield for a filter in lbs/hr/sf given the following information: Filter operates for 12 hours of each day and captures 95% of the influent solids. The solids load to the filter is 200 pounds per day. The filter is 40 feet square.
- 73. Coagulated raw water contains 120 mg/L of total suspended solids. The water plant produces 2.0 mgd and has two sand filters that are 20 feet wide by 20 feet long. If the filters operate 22 hours of each day and capture 99% of the coagulated solids, what is the filter yield in lbs/hr/sf? What is the filter yield total in pounds per day?
- 74. A series of filters discharge into a combined effluent trough. The trough is 5 feet wide by 80 feet long. A weir runs the full length of the trough. If the water plant capacity is 2 mgd, what is the weir overflow rate in gpd/sf?

Dilutions

- 75. A lab technician needs to make a 50 mg/L standard. Looking in the cabinet, they find a stock solution that is 1,000 mg/L. If the technician uses a 250 mL flask to make the standard, how many milliliters of stock solution will they need?
- 76. An arsenic standard is left sitting out on the counter without a lid for several days. In the beginning, the bottle had 150 mL of a 10,000 mg/L solution. After four days, the bottle only contained 120 mL. What is the new concentration of arsenic? Assume that arsenic does not evaporate.
- 77. Some polymer is being added to coagulate solids. It is added in the pipeline between the raw water intake and flocculation basin. The target dose is 25 mg/L and the influent flow rate is 7.74 cfs. If the raw chemical in the feeder tank is 5,000 mg/L, what should the pump rate be in gpm to achieve the desired dose.

- 78. Ferric chloride is being added as a coagulant to the raw water entering a plant. Sampling shows that the concentration of ferric in the raw water is 25 ppm. A quick check of the chemical metering pump shows that it is operating at a flow rate of 4.3 gpm. If the flow through the water plant is 800 gpm, what is the concentration of raw chemical in the dosing tank?
- 79. A water plant is fed by two different wells. The first well produces water at a rate of 600 gpm and contains arsenic at 0.5 mg/L. The second well produces water at a rate of 350 gpm and contains arsenic at 12.5 mg/L. What is the arsenic concentration of the blended water?
- 80. Liquid polymer is delivered as an 8 percent solution. How many gallons of liquid polymer should be mixed in a tank to produce 150 gallons of 0.6 percent solution?
- 81. There are two raw water lines feeding a water plant. One line carries a flow rate of 500 gpm with a TDS concentration of 1500 mg/L. The second line has a flow rate of 6 mgd with a a 250 mg/L TDS concentration. What is the actual combined TDS concentration entering the plant?
- 82. Two wells are used to satisfy demand during the summer months. One well produces water that contains 22 mg/L of Arsenic. The other well produces water that contains 3 mg/L of Arsenic. If the total demand for water is 400 gpm and the target Arsenic concentration in the finished water is 8 mg/L, what is the highest pumping rate possible for the first well?



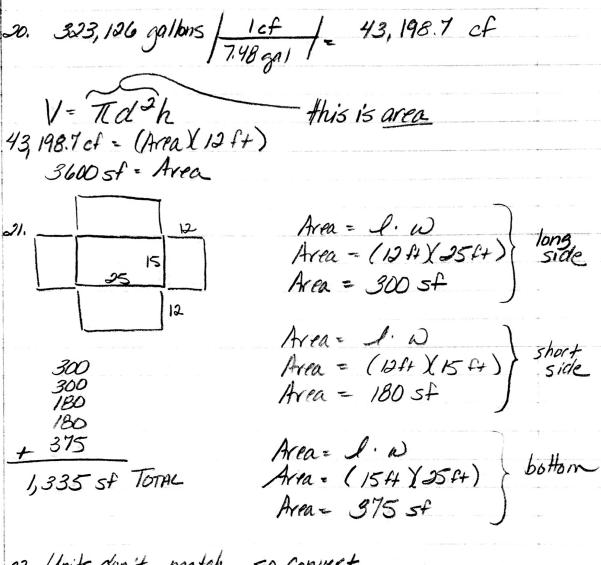


18. 6-inches = 0.5 ft V=0.185d2h V= (0.785)(0.5H)2(600f4) V= 117.75 cf 117.75 cf | 7.48 gal | = 881 gallons need 3 circles and 2 rectangles ACIRCLE = 0.785d2 ACIRCLE = (0.785 X 60f+)(60f+) ACIRCLE = 2826 ft2 x3 because we need 3 of them 8478 ft 2 pr lid + bottom ARECTANGE = LENGTH XWIDTH -height of must be equal to the perimete of the Perimeter or Circumference = Ta

Now instead of AREA = LENGTH & WIDTH WE gt

AREA = (CIRCUMPERENCE YWIDTH) AREA = (TLd X WIDTH) AREA = (3.14 X 60 f+ X 20 f+) AREA = 3768 SF x 2 because we need the inside + outside now add areas 8478 sf +7536sf The, 014 st to paint 20. V = 0.785 d2h 323,136 gallons = (0.785) (1) this needs to be in cubic feet so the units will







$$V_{TOP} = 0.785 d^{2}h$$

$$= (0.785)(24 + 4)^{2}(204+)$$

$$= 9043.2 cf$$

$$V_{BOTTOM} = \frac{0.785 d^2 h}{3}$$
= $(0.785)(24f+)^2(6f+)$
= $904.3 cf$



27. TIME = Vocume FIND VOLUME IN GALLONS Vocume = 0.785 d2h = (0.785 X 35 ft) (14 ft) = 13462.75 cf

13462.75 cf/14800/- 100,701

TIME = VOLUME

5 HRS = 100,701 gal

FLOW = 100,701 gal

FLOW = 20,140 gal

hr for gpm

20,140 gal 1 lhr / 336 gpm

28. V=1.w.h V= (504)(204)(8f+) V= 8,000 cf

9000cf [7.48 pl] 59840 gal

TIME = VOLUME FLOW TIME = 59,840gal 240gpm-TIME = 249 minutes

249 minutes is abo 4 hours 9 minutes





32.
$$V = 0.185 d^2 h$$
 12. $I = 14$
 $V = (0.785 \times 14)^3 (500 H)$
 $V = 392.5 cf$

$$Time = \frac{Volume}{Flow}$$
 $Time = \frac{785 cf}{30 cfm}$
 $Time = 26 minutes$

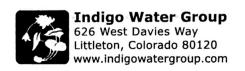


$$Tim \dot{\epsilon} = \frac{V}{Q}$$

$$5min = \frac{180.4 \text{ gal}}{Q}$$

$$(QX5) = (160.4)$$

$$Q = 36 \text{ gal}$$



39. FORCE = PRESSURE × AREA up until now, we've always converted inches into feet. With this equation we want inches because pressure it in pounds per square inch

AREA = 0.785 d2 = 113 in2

FORCE = Pressure × AneA = 0.185 (12 in) 2 FORCE = (60psi × 1/3 in 2) FORCE = 6782.4 lbs

6782.4 lbs 100 = 3.39 tons

40. AREA = 0.185 d2 = (0.785 X 42 inches)2 = 1,384 in 2

AREA = 0.785 N2 = (0.785 \ 10 inches)2 = 18.5 in2

FORCE = PXA FORCE = (BO psi X 1384 in2) FURCE = 110,779.2 165

FORCE = PXA FORCE = (80,51 X 78.51,2) FARCE = 6,280 165

110,779.216/ 1ton/= 55 tons

6,280 165 100 = 3.14 tons

41. 15 feet 10.433 Poil = 6.5 poil

FORCE = P.A -16.5psi X 28.26in2) = 183 165

AREA = (D.785 (N2) = (0.785 X6in)2 = 28.26 in 2



velocity is 4 times greater in 6-inch pipe



$$=(9H)(2++)$$



or - look up the conversion
$$lmgd = 1.55 cfs$$

then
$$2.5 mgd | 1.55 cfs | = 3.875 cfs$$

$$| lmgd | = 3.875 cfs$$

$$velocity = \frac{Q}{A}$$

$$velocity = \frac{3.875 cfs}{1sf}$$

$$velocity = 3.875 ffs$$

48.
$$HP = \frac{(gpm)(TDH,ft)}{3960}$$
 $HP = \frac{(120 gpm)(1200 ft)}{3960}$
 $HP = 36.4$

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WIRE TO WATER EFF. = WATER HP
$$\times$$
 100 motor HP = $\frac{6.31 \text{ HP}}{8.25 \text{ MP}} \times 100$ = $\frac{76.5\%}{100}$



55.
$$\frac{4inches}{12inches}$$
 $V = 0.785 d^{2}h$
 $V = (0.785)(0.33 ft)(0.67 ft)$
8 inches | 114 | 0.67 ft $V = 0.05/3 cf$ | stroke





61. how much does one gallon weigh?

50.00 (8.34 lbs × 5.25%) = 0.437 lbs C/2

62. 18 inches 1 ft | 1.5 ft.

Volume of Well = (0.785)(d)(h) Volume of Well = (0.785)(1.54)(80 ft) Volume of Well = 141,3 cf

141.3 cf | 7.48 gal | 1 mg |= 0.001056924 mg

FEED RATE, Ibs/day = (DOSE, mg/L & Capacity, mg & 8.34 bs/gal)

PURITY

FEED RATE, Ibs/d = (115 mg/L & 0.001056924 mg & 8.34 bs/gal)

0.0525

FEED PATE, lbs/d = 19.31
BUT, THEY ASKED FOR GALLONS OF BLEACH
19.31 lbs bleach | 1991/01 | = 2.3 gallons
day 8.34 lbs

- DAGE 24-





#65 REPRESE - you can also use the C, V, = C2 V2 formula to solve this problem

3.2 mg 1000000 get 3.785 L 1 day = 8411.11 mL day 1 mg 1 gal 1440min = 8411.11 mL

 $C,V_1 = C_2V_2$ $(642.3 \, mg/L \, \chi \, V_1) = (9 \, mg/L \, \chi \, 8411.11 \, mL/min)$ $(642.3 \, mg/L \, \chi \, V_1) = 75699.99$ $V_1 = 117.9 \, mL/min$

66. FEED RATE, gpm = (Plant Capacity, gpm X Doseage, MS/L)

FLED RATE, gpm = (400 gpm X 3 - 1.8 ms/L)

FEEDRATE, gpm = (400 gpm) 3 - 1.8 moll)
18,000 myll

FEED RATE, gpm = (400 gpm) 1.2 mg/L)

FEED RATE, gpm = 0.0267

67. Alum consumes 0.5 mg of alkalinity per mg of Alum

15 mg/Alum 10.5 Alkalinity = 7.5 mg/L Alkalinity used

- 7.5 ms/L Alkalinity remaining





40. PISE RATE, in/min = (BACKWHSH RATE, Jpm/sf / 12 inched/ft)
7.48 gal/cf 30 in/min = (BACKWASH, gpm/sf X 12 inches/ft) 224.4 = (BACKWASH, GPM/SFX /2 inches/ft) 18.7 gpm = BACKWASH, gpm/sf

H. Butend as if all flow is going to one filter

5.0 mg | 1000000 gal | 1 day | = 3472 gal min

AREA = I'W

AREA = (12 A+ X 20 A+)

AREA = 240sf

HLR = gpm

HLR = 3472 gpm 240 sf

HLR = 14,5 gpn/sf

3. I filter on-line



(400 st (2 filters) = 800 sf

FILTER YIELD, Ibs/M/sf = (solids, Ibld & 2 Recovery)

(operation, wold & Area, sf)

FILTER YIELD, Ibs/M/sf = (2001.6 Ibs/d & 0.99)

(22 hrs/d & 400 sf)

FILTER YIELD, Ibs/M/sf = 0.22518

gust take 165 (2001.6 × 0.99) = 1981.58 165/day





79.
$$C_1V_1 + C_2V_2 = C_3V_3$$

 $(0.5 \text{ mole} \times (0.00 \text{ gpm}) + (10.5 \text{ mole} \times (350 \text{ gpm}) = C_3(600 + 350 \text{ gpm})$
 $300 + 4375 = C_3(950)$
 $4675 = C_3(950)$
 $4,92 \text{ mole} = C_3$

80.
$$C, V_1 = C_2 V_2$$

 $(8\% X V_1) = (0.6\% X 150 gallons)$
 $(8\% X V_1) = 90$
 $V_1 = 11.25 gallons$



B) if
$$V_1 = V_1 + V_2$$

then $V_1 = V_3 - V_2$

$$C_{1}V_{1} + C_{2}V_{2} = C_{3}V_{3}$$

 $C_{2}V_{3}NLX400-V_{2}) + (3mg/LXV_{2}) = (8^{m}s/LX400 gpm)$
 $8800 - (19^{m}s/LXV_{2}) + (3mg/LXV_{2}) = 3200$
 $-(19^{m}s/LXV_{2}) = 3200 - 8800$
 $-(19^{m}s/LXV_{2}) = -5600$
 $(19^{m}s/LXV_{2}) = 5600$
 $V_{2} = 294.7 gpm$